

**Riga Technical University**

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# **STRUCTURAL RELIABILITY OF ELECTRICAL POWER SYSTEMS**

**Scientific Monograph**

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