

ALEKSANDRAS STULGINSKIS UNIVERSITY



THE SIXTH INTERNATIONAL SCIENTIFIC CONFERENCE

**RURAL DEVELOPMENT 2013**

**PROCEEDINGS**

**Volume 6, Book 3**

28–29 November, 2013  
Akademija

RURAL DEVELOPMENT 2013  
THE SIXTH INTERNATIONAL SCIENTIFIC CONFERENCE PROCEEDINGS  
Volume 6, Book 3

Aleksandras Stulginskis University  
Akademija, Kaunas district, Lithuania

**ISSN 2345-0916 (on line)**

**ISSN 1822-3230 (print)**

© Aleksandras Stulginskis University, 2013

Proceedings of the International Scientific conference "Rural Development 2013: Innovations and Sustainability" are indexed and abstracted in the international databases: Thomson Reuters ISI Web of Science (Conference Proceedings Citation Index), Academic Search Complete (EBSCO).

All papers published in the Proceedings of the International Scientific conference "Rural Development 2013: Innovations and Sustainability" have been peer reviewed by two experts in the field.

Conference website: [http://www.asu.lt/rural\\_\\_development/en](http://www.asu.lt/rural__development/en)

# Elliptical Guide Banks Scour: Equilibrium Stage

**Boriss Gjonsburgs, Gints Jaudzems, Elena Govsha**

*Riga Technical University, Latvia*

## Abstract

The damage of the bridge foundations, in the river flow, because of scour leads to considerable economic and environmental losses. The equilibrium stage of scour near guide banks with a uniform layer and stratified bed conditions have been studied. At present, no methods are available for computing the depth of a local scour near the bridge crossing structures under river bed layering. The aim of this study is to elucidate the influence of uniform bed and stratification on the scour depth at elliptical guide banks for clear water conditions on the plain rivers. Scour process is studied according to one of the cases proposed by Ettema (1980), when first layer or next one is fully scoured out.

The depth of scour considerably increases or reduces - depending on grain size of uniform layer and sequence, thickness of layers with different grain sizes. For example, the depth of scour is always greater when a fine-sand layer is under a coarse-sand layer(s) compare with the depth of scour obtained in coarse-sand layer with mean grain size, which is on the top of the river bed. A new method for computing the equilibrium scour depth at elliptical guide banks in uniform and stratified river bed conditions is presented. Equilibrium depth of scour can be calculated by proposed formulas in one or several bed layers with different mean grain size, thickness, and sequence combinations. The method is confirmed by test results. Calculation of the depth of scour at the bridge foundations in the flow and taking into account only the grain size diameter in the upper layer of the river bed, as it is accepted now, and neglecting stratification will lead to wrong results and finally to considerable damages and losses.

## Introduction

Streamline concentration, local increase in velocity, circulation and vortex structures, an increased turbulence, and a scour hole are observed at the head of guide banks. According to different authors, the depth of scour at bridge structures depends on the grain size of the surface layer of the river bed. But this approach does not reflect the complexity of the geological structure of river bed, which can increase the scour depth and cause damage to bridge structures.

The influence of the river bed stratification on the scour depth near bridge structures is confirmed by Rotenburg (1965), Ettema (1980), Raudkivi and Ettema (1983), and the others, but at present time there are no methods or formulas to calculate depth of scour at complex geological river bed conditions.

In this study, a new method for computing the equilibrium depth of scour at elliptical guide banks under uniform and stratified bed conditions is presented. According to experimental and calculation results, the depth of scour in uniform layer depends on grain size and in the stratified bed conditions, the depth of scour depends on the grain size of a layer, as well on thickness and sequence of the layers with different grain size. If the surface layer with a grain size  $d_1$  is scoured and the process is continued in the second layer with a grain size  $d_2$ , where  $d_1 < d_2$  and  $h_{equil} < H_{d1} + H_{d2}$  (the scour stops at the second layer), the scour depth in the case of two layers is the same as that in one layer with  $d_2$ . If the scour stops in the second layer and  $d_1 > d_2$ ,  $h_{equil} < H_{d1} + H_{d2}$ , its depth is greater than in the case of a uniform layer with a grain size  $d_1$ . Equilibrium depth of scour can be calculated by proposed formulas in bed layers with different mean grain size, thickness, and sequence combinations.

Calculation of the depth of scour at the bridge foundations in the flow and taking into account only the grain size diameter in the upper layer of the river bed, as it is accepted now, and neglecting stratification will lead to wrong results and finally to considerable damages and losses.

## Experimental Setup

The tests were carried out in a flume 3.5 m wide and 21 m long. The flow distribution between the channel and the floodplain was studied under open-channel flow conditions (Table 1). The rigid-bed tests were performed for different flow contractions and Froude numbers with the purpose of investigating the changes in velocity and water level near the embankment, along it, and near the modeled elliptical guide bank.

Table 1. Some experimental data for open flow conditions in a flume

Test	$L$ (cm)	$h_f$ (cm)	$V$ (cm/s)	$Q$ (l/s)	$Fr$	$Re_c$	$Re_f$
L1	350	7	6.47	16.60	0.0780	7500	4390
L2	350	7	8.58	22.70	0.10	10010	6060
L4	350	7	8.16	20.81	0.098	10270	5590/5660
L5	350	7	9.07	23.48	0.109	11280	6140/6410
L6	350	7	11.10	28.31	0.134	13800	7550/7840
L7	350	13	7.51	35.48	0.067	13700	9740
L8	350	13	8.74	41.38	0.076	16010	11395
L9	350	13	9.90	47.10	0.088	14300	14300

During sand-bed tests, the time-dependent changes in velocities and scour depth, the effect of different hydraulic parameters, the flow contraction rate, the grain size of bed materials, and the scour process were studied. The tests were performed in a flume of width  $L = 350\text{cm}$  for the following bridge-model openings: 50, 80, 120, and 200 cm. The flow contraction rate  $Q/Q_b$  (where  $Q$  is the general discharge and  $Q_b$  is the discharge through the bridge opening under open-flow conditions) varied from 1.56 to 5.69 for the floodplain depth  $h_f = 7$  and 13 cm, respectively; the Froude numbers varied from 0.078 to 0.134,  $Re_c$  – from 7500 to 16010, and  $Re_f$  – from 4390 to 14300, where  $Re_c$  and  $Re_f$  are the Reynolds numbers for the channel and floodplain, respectively; the slope of the flume was 0.0012.

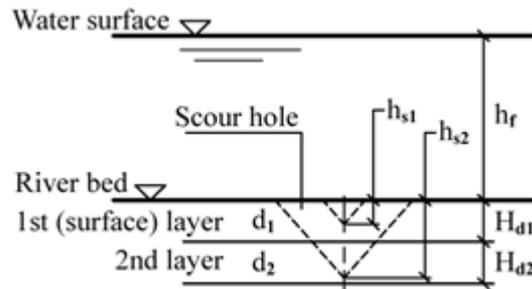


Figure 1. Geology of the river bed formed by layers with different grain sizes

The sand was placed 1 m up and down the contraction point of the flume. The grain sizes were 0.24 and 0.67 mm, and the tests were performed with a uniform layer or with two layers of different thicknesses and grain sizes. The dimension of the upper part of an elliptical guide bank, namely the length calculated according to the Latishenkov (1960) method and was found to be dependent on the flow contraction rate and the main channel width. The length of the lower part of the guide bank was assumed to be half of the upper part.

Scour process is studied according to one of the cases proposed by Ettema (1980), when first layer or next one is fully scoured out, and scour continue to develop in the next layer due to the new hydraulic conditions (Fig.2).

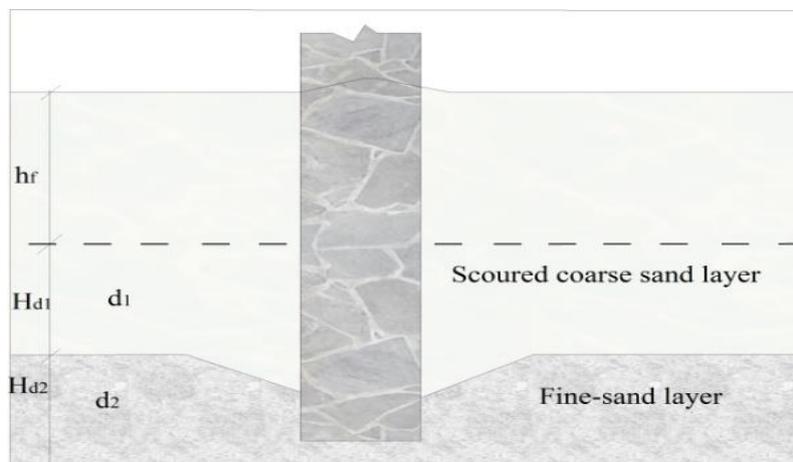


Figure 2. Scour in layered river bed, Case 11 (after Breusers and Raudkivi, 1991)

### Equilibrium depth of scour at uniform layer elliptical guide banks

The scour depth at elliptical guide banks is equal to the equilibrium depth in the conditions when the local velocity becomes equal to the critical one. The local velocity at a plain river bed is found by the Bernoulli equation for two cross sections of the extreme unit streamline [(Gjunsburgs and Neilands, 2004). The discharge across the width of a scour hole before and after the development of scour is  $Q_f = Q_{se}$ , where  $Q_f$  is the discharge across the width of a scour hole with the plain bed and  $Q_{se}$  is that with a depth  $h_{equil}$ .

$$m \cdot h_{equil} \cdot h_f \cdot V_{l_{el}} = \left( m \cdot h_{equil} h_f \frac{m \cdot h_{equil}}{2} h_{equil} \right) V_{lt} \quad (1)$$

where  $m$  is the steepness of the scour hole,  $h_{equil}$  is the depth of scour at the equilibrium stage,  $h_f$  is the depth of flow at the floodplain,  $V_{l_{el}}$  is the local velocity at plain river bed, and  $V_{lt}$  is local velocity at any depth of scour (Gjunsburgs et al. 2006). The local velocity  $V_{lt}$  at an equilibrium stage of scour is determined from Eq. (1)

$$V_{lt} = \frac{V_{l\,el}}{\left(1 + \frac{h_{equil}}{2h_f}\right)} \tag{2}$$

The critical velocity  $V_{0t}$  at the equilibrium stage can be determined through the mean depth of flow  $h_m = h_f(1+h_{equil}/2h_f)$  near elliptical guide banks at that stage:

$$V_{0t} = \beta \cdot 3.6d_i^{0.25} h_f^{0.25} \left(1 + \frac{h_{equil}}{2h_f}\right)^{0.25} \tag{3}$$

where  $\beta$  is a coefficient of reduction in the critical velocity due to vortex structures,  $d_i$  is the grain size of the bed materials, and  $V_0 = 3.6d_i^{0.25} h_f^{0.25}$  is the critical velocity at the plain bed (Studenichnikov 1964).

The scour at the equilibrium stage stops when the local velocity  $V_{lt}$  (Eq. 2) becomes equal to the critical velocity  $V_{0t}$  (Eq. 3)

$$\frac{V_{l\,el}}{\left(1 + \frac{h_{equil}}{2h_f}\right)} = \beta \cdot 3.6d_i^{0.25} h_f^{0.25} \left(1 + \frac{h_{equil}}{2h_f}\right)^{0.25} \tag{4}$$

From Eq. 4, the equilibrium depth of scour at elliptical guide banks is found

$$h_{equil} = 2h_f \left[ \left( \frac{V_l}{\beta V_0} \right)^{0.8} - 1 \right] \cdot k_\alpha \cdot k_m \tag{5}$$

where  $k_\alpha$  is a coefficient depending on the flow crossing angle and  $k_m$  is a coefficient depending on the side-wall slope  $zszx$  of guide banks. According to Eq. (5), the equilibrium depth of scour depends on the floodplain depth, contraction rate of flow, backwater value, and the grain size of river bed. With increase in the grain size, the equilibrium depth of scour reduces.

**Equilibrium depth of scour at stratified bed at elliptical guide banks**

Geology of the river bed is complicate and usually has layers with different thickness and grain sizes (Fig. 3).

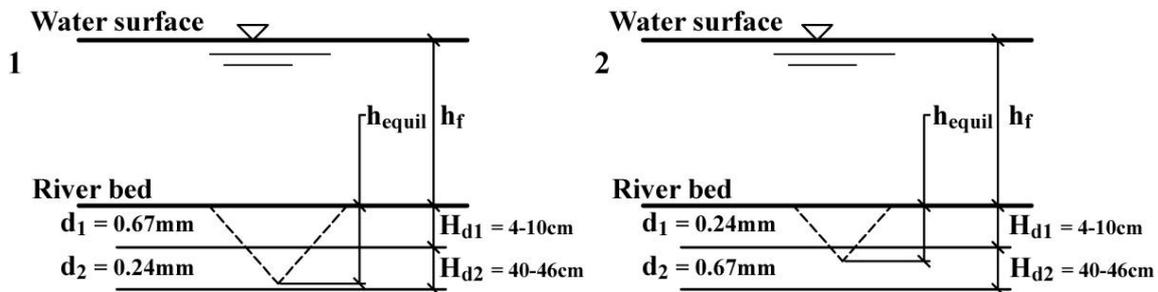


Figure 3. Two layers with different test grain sizes

When the scour depth  $h_{equil} < H_{d1}$ , equation (5) can be used; however, when  $h_{equil} > H_{d1}$ , the scour develops in the second layer with a grain size  $d_2$ . If  $h_{equil} > H_{d1} + H_{d2}$ , the scour develops in the third layer with a grain size  $d_3$ , and so on. Then, the equilibrium scour depth is different from that in the uniform layer. At the initial stage, the equilibrium scour depth  $h_{equil}$  is calculated by Eq. (5). When  $h_{equil} > H_{d1}$ , the scour develops in the second layer with  $d_2$ . Now, to determine the equilibrium depth of scour the local and critical velocities on the top of the second layer must be calculated. The local velocity on the surface of the second layer is found by the formula

$$V_{lt1} = \frac{V_{l\,el}}{\left(1 + \frac{H_{d1}}{2h_f}\right)} \tag{6}$$

where  $H_{d1}$  is the thickness of the first layer of the river bed.

The critical velocity is determined from the medium depth of flow  $h_{mid} = h_f(1+H_{d1}/2h_f)$  on the floodplain with a scour depth equal to the thickness of the first bed layer,

$$V_{01} = \beta 3.6 \cdot d_2^{0.25} h_f^{0.25} \left(1 + \frac{H_{d1}}{2h_f}\right) \tag{7}$$

where  $V_0 = \beta 3.6d_2^{0.25} h_f^{0.25}$  is the critical velocity of flow for the grain size  $d_2$ , since the layer with exactly this diameter lies on the top of the river bed. Then, the scour depth in the second layer is determined as

$$h_{s2} = 2h_f \left[ \left( \frac{V_{lt1}}{V_{01}} \right)^{0.8} - 1 \right] \cdot k_\alpha \cdot k_m \tag{8}$$

At  $h_{s2} < H_{d2}$ , the scour stops, and the equilibrium scour depth is

$$h_{equil} = H_{d1} + h_{s2} \tag{9}$$

If  $h_{s2} > H_{d2}$ , the calculation could be continued using Eq. (8).

**Results**

The flow pattern at the head of the elliptical guide banks is modified. As it was found in the tests, the streamlines are bended, flow velocities reduce almost to zero when flow approaching the bridge crossing embankments and then gradually increases. At the head of the elliptical guide banks the concentration of streamlines, a sharp drop in water level, a local increase in the velocity, and circulation was observed (Gjunsburgs et al. 2004). Locally modified flow near the guide banks is forming the local scour hole.

The local velocity  $V_{lt}$  reduces more rapidly if the second layer has grains of a smaller size. Depending on the layers grain size, the critical velocity  $\beta V_{0t}$  either increases, when the grains of the second layer are coarser, or reduces, when these grains of the second layer are finer.

The test results are presented in Table 2. The EL 4-6 tests were performed with one uniform layer with a mean diameter of 0.24 mm, the EL16-18 tests with a mean diameter of 0.67mm, and the EUL 1-6 tests were carried out with two layers of different thickness with grain sizes  $d_1 = 0.24$  mm and  $d_2 = 0.67$  mm.

Table 2. Test results for elliptical guide banks

Test	$\frac{Q}{Q_b}$	$d_1$ (mm)	$d_2$ (mm)	$H_{d1}$ (cm)	$H_{d2}$ (cm)	$t$ (h)	$h_{s\ test}$ (cm)	$h_{s\ calc}$ (cm)	$\frac{h_{s\ test}}{h_{s\ calc}}$	$h_{equil}$ ( $d_1$ ) (cm)	$h_{equil}$ ( $d_2$ ) (cm)	$h_{equil}$ (layers) (cm)
EL4	3.66	0.24	-	50	-	7	7.6	8.40	0.905	10.43	-	-
EL5	3.87	0.24	-	50	-	7	11.0	11.00	1.000	14.10	-	-
EL6	3.78	0.24	-	50	-	7	14.0	13.51	1.036	17.65	-	-
EL16	3.66	0.67	-	50	-	7	6.1	5.60	1.084	5.90	-	-
EL17	3.87	0.67	-	50	-	7	8.4	8.35	1.005	8.91	-	-
EL18	3.78	0.67	-	50	-	7	12.2	10.50	1.162	11.78	-	-
EUL1	3.66	0.67	0.24	4	46	7	8.2	8.48	0.966	5.90	10.43	10.43
EUL2	3.87	0.67	0.24	7	43	7	10.7	10.85	0.986	8.91	14.10	14.10
EUL3	3.78	0.67	0.24	10	40	7	12.4	11.97	1.035	11.78	17.65	17.65
EUL4	3.66	0.24	0.67	4	46	7	5.6	5.74	0.975	10.43	5.90	5.90
EUL5	3.87	0.24	0.67	7	43	7	8.6	8.44	1.018	14.10	8.91	8.91
EUL6	3.78	0.24	0.67	10	40	7	11.4	11.03	1.033	17.62	11.78	11.78

The opening of the bridge model was 80 cm and the floodplain depth was 7 cm. The tests lasted for 7 hours. The scour depth developed in 7 hours was prolonged to an equilibrium stage by using the method elaborated by Gjunsburgs et al (2007). The equilibrium scour depth in tests with uniform layer was respectively 10.43, 14.10, and 17.65 cm with mean grain-size diameters 0.24 mm and 5.90 cm and 8.91 cm and 11.78 cm with a 0.67 mm diameter. The Froude numbers of the open flow were 0.078, 0.104, and 0.124. The tests with two layers were performed for different thicknesses and grain sizes of layers. In the EUL1, EUL2, and EUL3 tests, the first and the second layers had grain sizes of 0.67 and 0.24 mm, respectively. When the layer was scoured and  $h_s > H_{d1}$ , the equilibrium scour depth, both determined in tests and calculated by Eq. (8), was the same if one layer had  $d_1 = 0.24$  mm. This fact evidences the important role played by the grain size of the second layer,  $d_2 = 0.24$  mm; the depth of scour increases rapidly in the second layer ( $d_2 < d_1$ ) in spite of the presence of the upper layer with diameter  $d_1 = 0.67$  mm. The calculated depth of scour with the grain size existing on the bed surface gives smaller values. In the EUL4, EUL5, and EUL6 tests, the first layer had the grain size  $d_1 = 0.24$  mm and the next layer had  $d_2 = 0.67$  mm. When the first layer was scoured and  $h_s > H_{d1}$ , the equilibrium depth of scour became equal to that found for one layer with the grain size 0.67 mm. The determined equilibrium depth of scour was smaller than that used in the formulae with  $d_1 = 0.24$  mm on the surface. As follows from experimental results and the method presented, the dominant grain size for calculating the depth of scour at elliptical guide banks under stratified bed conditions is the mean diameter of the second layer or of any next layer where the scour stops.

Dependence on the sequence of layers, ratio of velocities, the Froude numbers of the open flow,  $Fr$ , the Froude number with a local velocity at the head of elliptical guide banks,  $Fr_{vl}$ , the Froude number at the end of the tests, with a depth of scour  $h_s$ ,  $Fr_{vlr}$ , the densimetric Froude number, and the densimetric Froude number at the guide banks with a local velocity,  $Fr_{dl}$ , on relative depth of scour is found.

The equilibrium depth of scour is always greater if the coarse-grain layer lies on the top of the river bed and a fine-grain layer goes after it, and the depth is smaller if the fine-grain layer lies on the surface of the river bed.

## Conclusions

The equilibrium stage of scour at guide banks under uniform and stratified bed conditions have been studied. The method for computing the equilibrium depth of scour under these conditions is presented (Eq. 8). The method is confirmed by test results (Table 1). According to the method and test results, the equilibrium depth of scour at elliptical guide banks strictly depends on the sequence of the bed layers with different grain sizes. When the first uniform coarse sand layer is scoured  $h_s > H_{dl}$  (Fig. 2), the equilibrium depth of scour becomes equal to its value achieved in the second uniform fine sand layer with a grain size  $d_2$ . If the first fine sand layer is scoured (Fig. 2), the equilibrium scour depth is equal to that in the second coarse sand layer (Table 1). In the stratified bed conditions, the use of grain-size parameters of the river bed material on the surface for calculating the equilibrium scour depth yields incorrect results. The most critical conditions for structures appear when a fine-sand layer occurs under a coarse-sand layer. As soon as the coarse layer has been scoured out, the scour is rapidly developing in the next, fine-sand one. In this case, the dominant value of grain size for computing the depth of scour at elliptical guide banks under stratified bed conditions is the mean diameter of the second layer or of the next one, where the scour stops. According to the results, the depth of scour is always greater when a fine-sand layer is under a coarse-sand layer(s) compare with the depth of scour obtained with mean grain size which is on the top of the river bed. The calculation of scour depth near bridge structures in flow by using only the mean grain size diameter on top of the river bed and neglecting the stratification, as it is excepted now, can lead to wrong results and finally to considerable damages and losses.

## References

1. Ettema, R. E. Scour at bridge piers. University of Auckland, New Zealand, 1980, Report 236.
2. Gjunsburgs, B., Neilands, R.R., Govsha, E. Local Scour at Elliptical Guide Banks in Plain Rivers. Proc. of River Flow 2006, Lisbon, Portugal, 2006, Vol.2, pp. 1649-1655.
3. Gjunsburgs, B., Neilands, R.R., Govsha E. Scour development at elliptical guide banks during multiple floods. Proc. of 32<sup>nd</sup> Congress of IAHR, Venice, Italy, 2007, Vol.2, pp 598-608.
4. Gjunsburgs, B. & Neilands, R. Local velocity at bridge abutments on plain rivers. Proc. River Flow 2004, in Greco, Carravetta & Della Morte (eds), Napoli, Italy, 2004, Vol.1, pp 443-448.
5. Raudkivi, A. J., Ettema, R. E. Clear water scour at cylindrical piers. Journal of Hydraulic Engineering, No.3 (109), 1983, pp. 338-35.
6. Rotenburs, I.S., Polykov, M.P., Zolotarev, I.V., Lavrovskji, V.A. Bridge crossing design. Moscow: Vysshaya Shkola (in Russian), 1965.
7. Studenichnikov B. Scouring Capacity of Flow and Methods of Channel Calculation. Moscow: Stroiizdat, 1964.

---

**Boriss GJUNSBURGS**, Prof., Water engineering and technology department, Riga Technical University, Azenes 16-261, Riga, LV-1048, Latvia, e-mail: gjunsburgs@mail.bf.rtu.lv

**Gints JAUDZEMS**, PhD student, Water engineering and technology department, Riga Technical University, Azenes 16-261, Riga, LV-1048, Latvia, e-mail: gints.jaudzems@rtu.lv

**Elena GOVSHA**, PhD student, Water engineering and technology department, Riga Technical University, Azenes 16-261, Riga, LV-1048, Latvia, e-mail: jelena.govsa@rtu.lv